Sylabusy - Centrum Informatyczne U



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Course contents				-			
	Course contents						

1. Topological and differentiable manifolds, charts, atlas and differential structure.

2. Maps between manifolds, the rank of the map.



	 Skills Student who completed the course: is able to solve basic problems stated by calculus on manifolds by means of standard methods of calculus, algebra and topology, as well as definitions and 				
pecialization)	 Student who completed the course: knows basic definitions and formulate of calculus (analysis) on manifolds; knows examples and counterexamples of defined objects; correctly states and proves basic theorems of calculus on manifolds. M2_W01, M2_W02, M2_W03 				
 John Milnor, "Topology from the differentiable viewpoint" Michael Spivak, "Calculus on manifolds" he learning outcomes (for the field of study and pacialization) 	Knowledge				
 Morris W. Hirsch, "Differential Topology", Springer 					
bibliography of literature					
 The degree of the map. Forms on manifolds, integration on manifolds and Stol 					
8. Manifolds with boundary.					
7. Orientation of manifold.					
 Tangent space and tangent bundle, the derivative of the Transversality. 	map between manifolds.				
Immersions, submersions, embeddings.					